

- (1) Consider the vector field  $F(x, y) = (2x/y, (1 - x^2)/y^2)$  for  $y > 0$ .
- (a) Check that  $F$  is potential (conservative) and find a potential function
- (b) Let  $C$  be the curve  $(x - 3)^5 + y^2 = 3$ , from  $(2, -2)$  to  $(2, 2)$ . Compute  $\int_C \vec{F} \cdot d\vec{r}$ .
- (2) Evaluate  $\int_C F \cdot dr$  where

$$F(x, y) = \left( \frac{1}{y^2 + 1}, -\frac{2xy}{(y^2 + 1)^2} + ze^{yz}, ye^{yz} + 2z \right)$$

where  $C$  is part of the helix  $r(t) = \langle \cos(t), \sin(t), t \rangle$  from  $(1, 0, 0)$  to  $(1, 0, 2\pi)$ .

- (3) Find the integral of  $f(x, y) = x^2 + y^2$  on the domain
- $$D := \{(x, y) \in \mathbb{R}^2 : 0 \leq x \leq 1, x^2 \leq y \leq x\}.$$

Sketch the region of integration.

- (4) Find the limits of integration of  $\iint_D f(x, y) dx dy$  if

$$D := \{(x, y) \in \mathbb{R}^2 : \frac{x^2}{9} + \frac{y^2}{4} \leq 1\}$$

when  $D$  is considered first as a type I and then as a type II domain.

- (5) Sketch the region bounded by the curves  $y = \log(x)$ ,  $y = 2\log(x)$  and  $x = e$  in the first quadrant. Then express the region's area as an iterated double integral and evaluate.
- (6) Consider  $\iint_D f dA = \int_0^3 \int_{-2\sqrt{1-(x/3)^2}}^{2(1-x/3)} f(x, y) dy dx$ .
- (a) Sketch the region of integration.
- (b) Switch the order of integration in the above integral.
- (c) Compute the integral  $\iint_D f dA$  if  $f(x, y) = xy$ .

- (7) <sup>1</sup> Suppose  $f$  is a continuous invertible function from  $[0, 1]$  to  $[0, 1]$  such that  $f(0) = 0$ ,  $f(1) = 1$  and  $\int_0^1 f(x) dx = 1/6$ . Let  $g$  denote the inverse function. Evaluate  $\int_0^1 g(x) dx$ .

<sup>1</sup>Not to appear on the quiz.