CHRISTOPHER J. BISHOP

Department of Mathematics Stony Brook University Stony Brook, NY 11794-3651

RESEARCH INTERESTS

Real and complex analysis, geometric function theory, conformal dynamics, probability theory, numerical analysis, analysis on fractals, quasiconformal geometry, computational geometry.

Some of my more particular interests have included: potential theory, fractal properties of harmonic measure, geometric properties of Brownian motion and other random processes, algebras generated by harmonic and holomorphic functions, geometry of hyperbolic manifolds and their covering groups, numerical computation of conformal mappings, multipole methods, optimal meshing algorithms, nonobtuse triangulation, quadrilateral meshing, iteration of entire functions, the geometry of Weil-Petterson quasicircles and their relation to energy functionals, mininal surfaces and renormalized area. I program in C, Mathematica and Matlab as part of my investigations in these areas, and teach a class on experimental aspects of mathematics.

PROFESSIONAL EXPERIENCE

Nov. 2021 to present: SUNY distinguished professor at Stony Brook University.

- Sept. 1997 to Nov. 2021: Full professor at Stony Brook.
- Sept. 1992 to Aug. 1997: Assoc. professor at Stony Brook.
- Sept. 1991 to Aug. 1992: Asst. professor at Stony Brook.
- Sept. 1988 to Aug. 1991: Hedrick Asst. professor at UCLA.
- Sept. 1987 to Aug. 1988: NSF postdoc at MSRI, Berkeley.

EDUCATION

Cambridge University, Master of Advanced Study (MASt), 2011.
University of Chicago, Mathematics, Ph. D., 1987, Advisor Peter W. Jones.
Visiting graduate student and programmer, Dept. of Mathematics, Yale University, 1985-1987.
University of Chicago, Mathematics, Master of Science, 1984.
Cambridge University, Certificate of Advanced Study (Part III of Math. Tripos), 1983.
Michigan State University, Mathematics, Bachelor of Science, 1982.

PH.D. STUDENTS

Zsuzsanna Gonye, Ph. D. 2001, Geodesics in hyperbolic manifolds, Assoc. Professor, Eötvös Lorand University Karyn Lundberg, Ph. D. 2005, Boundary behavior of conformal mappings, researcher, Lincoln Labs Hrant Hakobyan, Ph.D. 2007, Hausdorff dimension and quasisymmetric mappings, Assoc. Professor, Kansas State University

Chris Green, Ph.D. Dec. 2011, Ahlfors iteration for numerical conformal mapping, senior researcher at Twitter

Kirill Lazebnik , Ph.D. August 2017, Wandering domains for the Eremenko-Lyubich class, assistant professor at Univ. North Texas

Jack Burkart, Ph.D May 2021, Packing dimension of transcendental Julia sets, Postdoc at Univ. Wisconsin, Madison

Alex Rodriguez, current student, quasiconformal constructions in analysis

POSTDOCS AND VISITORS

Maria Victoria Meliáan, 1994-1995 Torbjorn Lundh, 1996-1998

Jeremy Tyson, 1999-2002 Luke Rogers, Spring 2004 Mathew Badger, 2011-2014 Yaar Solomon, 2013-2016 Malik Younsi, 2014-2016 Simon Albrecht, Spring 2016 Dimitrios Ntalampekos, 2018-2021 Peter Lin, 2019-2022 Christina Karafyllia, 2019-2021 Matthew Romney, 2020-2023 James Waterman, 2021-2024

RECENT UNDERGRADUATE THESES AND RESEARCH

Ahmad Rafiqi, Summer 2011, Estimating conformal maps with accelerated random walks, Ph.D. program at Cornell.

Kevin Sackel, 2012-13, Geometric problems related to removability, Churchill Scholar at University of Cambridge, Ph.D. program MIT, postdoc at Stony Brook starting Fall 2019.
Abraham Rabinowitz, 2013-2014, Real Analysis, Ph.D. program at Northwestern.
Luke Green 2012-13, Real Analysis, data scientist for Openslate.
Jackson Rudd, Spring 2013, Functional Analysis, data intern for Disney/ESPN.

Shalin Parekh, 2014-15, Small dimension paths in the Brownian trace, one of ten students accepted special year in probability at University of Geneva run by Smirnov and Werner, currently in Ph.D. program at Columbia.

Christopher Dular, Fall 2015, Refining a triangulation to nonobtuse triangulation, masters program Georgia Tech.

William Vickery, Fall 2016, Generating random permutations using transpositions, Ph.D. program Northwestern.

Ray Zhang, Fall 2017, Functional analysis and machine learning, finance industry.

Joseph Suk, Fall 2017, Numerical approximation of shapes by dessins d'enfants, attending Carnegie-Mellon Ph.D. program.

Yugarshi Mondal, Spring 2018, Schramm-Loewner Evolutions.

Emi Brawley, Fall 2018, Kakeya sets, attending UC Davis PhD program in Fall 2019.

Hindy Drillick, Spring 2019, Removable sets and dimension, attending Columbia Ph.D. program in Fall 2019.

Luke Russo, Fall 2022, Riemann surfaces and Belyi's theorem, Ph.D. program at UCLA.

Sean Andrade Spring 2024, Simons STEM Scholar, current undergraduate

Ao Yi Spring/Fall 2024, Masters student, harmonic mesure.

RECENT SERVICE

Department

Chairman's Advisory Committee.

Professional development seminar for PhD students and postdocs.

Search committee.

Graduate committee.

Hiring committee.

Simons lecture committee.

Math day lecturer/organizer.

Comprehensive exam writer/grader.

Former associate chair of math department.

Former assistant director of Institute for Mathematical Sciences.

University

Organizer SCGP Spring School in Discrete and Computational Geometry, April 2017. SBU Center for Finance committee.

Search committee for Frey chair in quantitative finance.

Mentor for senior honors theses.

Outside University

Editorial Board, AMS University Lecture Series

Editoral Board, Annales Fennici Mathematici

Reviewer for various journals and *Math. Reviews.* NSF panelist and reviewer. Lecturer for Center for Talented Youth Program. Organizer for Special Section as AMS sectional meeting, Spring 2016. Organizer for International Research Symposium, KIAS Seoul South Korea, April 2017. Outside hiring referee, Jyväskylä University. Outside dissertation referee, Jyväskylä University. Outside dissertation referee, Tel Aviv University. Outside dissertation referee, University of South Australia. Various promotion evaluations and letters.

AWARDS

London Math. Society, Senior Berwick Prize, 2024.

SUNY Distinguished professor, 2020.

Simons Fellow, 2019-20.

Fellow of the American Mathematical Society, 2019.

Invited speaker at 2018 ICM, Rio de Janeiro.

NSF standard grants (1991-present): DMS 91-00671, DMS 92-04092, DMS 95-00577, DMS 98-00924, DMS 01-03626, DMS 04-05578, DMS 07-05455, DMS 10-06309, DMS 13-05233, DMS 16-08577, DMS 19-06259, DMS 23-03987. Recent proposal reviews available on personal website.

1992 Alfred P. Sloan Research Fellow

1987-91 NSF Postdoctoral Fellowship

1983-1986 McCormick Fellowship, NSF Fellowship, U. of Chicago

1982-1983 Churchill Fellowship, Cambridge England.

PUBLICATIONS

- C. J. Bishop and J. K. Wetterer Planktivore prey selection: the relative field volume model vs. the apparent size model. *Ecology*, 66(2):457, 1985.
- [2] C. J. Bishop. A counterexample in conformal welding concerning Hausdorff dimension. Michigan Math. J., 35(1):151–159, 1988.
- [3] C. J. Bishop. An element of the disk-algebra that is stationary on a set of positive length. Algebra i Analiz, 1(3):83–88, 1989.
- [4] C. J. Bishop. Constructing continuous functions holomorphic off a curve. J. Funct. Anal., 82(1):113–137, 1989.
- [5] C. J. Bishop. Approximating continuous functions by holomorphic and harmonic functions. *Trans. Amer. Math. Soc.*, 311(2):781–811, 1989.
- [6] C. J. Bishop, L. Carleson, J. B. Garnett, and P. W. Jones. Harmonic measures supported on curves. *Pacific J. Math.*, 138(2):233–236, 1989.

- [7] C. J. Bishop. Bounded functions in the little Bloch space. *Pacific J. Math.*, 142(2):209–225, 1990.
- [8] C. J. Bishop. Conformal welding of rectifiable curves. Math. Scand., 67(1):61–72, 1990.
- [9] C. J. Bishop and P. W. Jones. Harmonic measure and arclength. Ann. of Math. (2), 132(3):511–547, 1990.
- [10] C. J. Bishop and T. Steger. Three rigidity criteria for PSL(2, R). Bull. Amer. Math. Soc. (N.S.), 24(1):117–123, 1991.
- [11] C. J. Bishop. A characterization of Poissonian domains. Ark. Mat., 29(1):1–24, 1991.
- [12] C. J. Bishop. Brownian motion in Denjoy domains. Ann. Probab., 20(2):631–651, 1992.
- [13] C. J. Bishop. Some questions concerning harmonic measure. In Partial differential equations with minimal smoothness and applications (Chicago, IL, 1990), volume 42 of IMA Vol. Math. Appl., pages 89–97. Springer, New York, 1992.
- [14] C. J. Bishop and T. Steger. Representation-theoretic rigidity in PSL(2, R). Acta Math., 170(1):121–149, 1993.
- [15] C. J. Bishop. An indestructible Blaschke product in the little Bloch space. Publ. Mat., 37(1):95–109, 1993.
- [16] C. J. Bishop. How geodesics approach the boundary in a simply connected domain. J. Anal. Math., 64:291–325, 1994.
- [17] C. J. Bishop and P. W. Jones. Harmonic measure, L² estimates and the Schwarzian derivative. J. Anal. Math., 62:77–113, 1994.
- [18] C. J. Bishop. Some homeomorphisms of the sphere conformal off a curve. Ann. Acad. Sci. Fenn. Ser. A I Math., 19(2):323–338, 1994.
- [19] C. J. Bishop. A counterexample concerning smooth approximation. Proc. Amer. Math. Soc., 124(10):3131–3134, 1996.
- [20] C. J. Bishop. A distance formula for algebras on the disk. Pacific J. Math., 174(1):1–27, 1996.
- [21] C. J. Bishop. Minkowski dimension and the Poincaré exponent. Michigan Math. J., 43(2):231–246, 1996.
- [22] C. J. Bishop. On a theorem of Beardon and Maskit. Ann. Acad. Sci. Fenn. Math., 21(2):383–388, 1996.
- [23] C. J. Bishop. Some characterizations of C(M). Proc. Amer. Math. Soc., 124(9):2695–2701, 1996.
- [24] C. J. Bishop. Geometric exponents and Kleinian groups. Invent. Math., 127(1):33–50, 1997.
- [25] C. J. Bishop and Y. Peres. Packing dimension and Cartesian products. Trans. Amer. Math. Soc., 348(11):4433–4445, 1996.
- [26] C. J. Bishop and Peter W. Jones. Hausdorff dimension and Kleinian groups. Acta Math., 179(1):1–39, 1997.

- [27] C. J. Bishop and P. W. Jones. The law of the iterated logarithm for Kleinian groups. In Lipa's legacy (New York, 1995), volume 211 of Contemp. Math., pages 17–50. Amer. Math. Soc., Providence, RI, 1997.
- [28] C. J. Bishop and P. W. Jones. Wiggly sets and limit sets. Ark. Mat., 35(2):201–224, 1997.
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- [30] C. J. Bishop. Quasiconformal mappings which increase dimension. Ann. Acad. Sci. Fenn. Math., 24(2):397–407, 1999.
- [31] C. J. Bishop. A quasisymmetric surface with no rectifiable curves. Proc. Amer. Math. Soc., 127(7):2035–2040, 1999.
- [32] C. J. Bishop, A. Böttcher, Yu. I. Karlovich, and I. Spitkovsky. Local spectra and index of singular integral operators with piecewise continuous coefficients on composed curves. *Math. Nachr.*, 206:5–83, 1999.
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- [34] C. J. Bishop and J. T. Tyson. Locally minimal sets for conformal dimension. Ann. Acad. Sci. Fenn. Math., 26(2):361–373, 2001.
- [35] C. J. Bishop. Bi-Lipschitz homogeneous curves in ℝ² are quasicircles. Trans. Amer. Math. Soc., 353(7):2655–2663 (electronic), 2001.
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- [37] C. J. Bishop. BiLipschitz approximations of quasiconformal maps. Ann. Acad. Sci. Fenn. Math., 27(1):97–108, 2002.
- [38] C. J. Bishop. Quasiconformal mappings of Y-pieces. Rev. Mat. Iberoamericana, 18(3):627– 652, 2002.
- [39] C. J. Bishop. Non-rectifiable limit sets of dimension one. Rev. Mat. Iberoamericana, 18(3):653–684, 2002.
- [40] C. J. Bishop and P. W. Jones. Compact deformations of Fuchsian groups. J. Anal. Math., 87:5–36, 2002. Dedicated to the memory of Thomas H. Wolff.
- [41] C. J. Bishop. Quasiconformal Lipschitz maps, Sullivan's convex hull theorem and Brennan's conjecture. Ark. Mat., 40(1):1–26, 2002.
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- [52] C.J. Bishop and H. Hakobyan. A central set of dimension 2. Proc. Amer. Math. Soc., pages 2453-2461, 136(2008), no. 7.
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- [55] C.J. Bishop. A set containing rectifiable arcs locally but not globally. Pure and Applied Math. Quarterly, 7(1): 121-138, 2011. Special issue in honor of Fred Gehring, part 1 of 2.
- [56] C.J. Bishop. Conformal mapping in linear time. Discrete and Computational Geometry, 44(2) 330-428, 2010.
- [57] C.J. Bishop. Bounds for the CRDT algorithm. Computational Methods in Function Theory, 10(1): 325-366, 2010.
- [58] C.J. Bishop. Optimal angle bounds for quadrilateral meshes. Discrete and Computational Geometry, 44(2): 308-329, 2010.
- [59] C.J. Bishop. Tree-like decompositions and conformal maps. Annals Acad. Sci. Fenn., 35(2): pages 389-404, 2010.
- [60] C.J. Bishop. A random walk in analysis. In the collection All That Math: portraits of mathematicians as young readers, 2011, a special volume of Revisita Matematica Iberoamericana, celebrating the Centennial of the Real Sociedad Matematica Espanola, Edited by Antonio Cordoba, Jose L. Fernandez and Pablo Fernandez
- [61] C.J. Bishop. True trees are dense. Invent. Mat. 197(2): pages 433-452, 2014.
- [62] C.J. Bishop with E. Feinberg and J. Zhang. Examples concerning Abel and Cesaro limits. J. Math. Analysis and App., 420(2): pages 1654-1661, 2014.
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- [64] C.J. Bishop. Constructing entire functions by quasiconformal folding. Acta. Math., 214(1): pages 1–60, 2015.

- [65] C.J. Bishop and K. Pilgrim. Dynamical dessins are dense. Rev. Mat. Iberoamericana, 31(3): pages 1033-1040, 2015.
- [66] C.J. Bishop. Models for the Eremenko-Lyubich class J. London Math. Soc., 92(1): 202-221, 2015.
- [67] C.J. Bishop. Nonobtuse triangulations of PSLGs Discrete and Computational Geometry, 56(1): pages 43–92, 2016.
- [68] C.J. Bishop. Quadrilateral meshes for PSLGs Discrete and Computational Geometry, 56(1): pages 1–42, 2016.
- [69] C.J. Bishop, H. Hakobyan and M. Williams. Frequency of dimension distortion under quasisymmetric mappings, *Geometric and Functional Analysis (GAFA)*, 26(2): pages 379–421, 2016.
- [70] C.J. Bishop. Models for the Speiser class. Proc. London Math. Soc., 114(3), 765–797, 2017.
- [71] C.J. Bishop. A transcendental Julia set of dimension 1. Inventiones Math., 212(2), 407–460, 2018.
- [72] C.J. Bishop and C. LeBrun. Anti-Self-Dual 4-manifolds, Quasi-Fuchsian groups and almost-Kahler geometry Comm. in Analysis and Geometry, special issue dedicated to Karen Uhlenbeck, 28(4), 745–780, 2020.
- [73] C.J. Bishop and K. Lazebnik. Prescribing the Postsingular Dynamics of Meromorphic Functions, Math. Annalen, 375(3), 1761-1782, 2019.
- [74] C.J. Bishop and S. Albrecht. A Speiser class Julia set with dimension near one, Journal d'Analyse, special issue dedicated to Larry Zalcman, 141(1), 49–98, 2020.
- [75] C.J. Bishop, H. Drillick and D. Ntalampekos. Falconers' distance set conjecture can fail for strictly convex sets in \mathbb{R}^d . Revista Mat. Iberoamericana, 37(5), 1953–1968, 2021.
- [76] C.J. Bishop. Quasiconformal maps with thin dilatations. Publications Matemàtiques vol 66(2022), 715-727.
- [77] C.J. Bishop. Conformal images of Carleson curves. Proc. Amer. Math. Soc. 9 (2022), 90–94.
- [78] C.J. Bishop. The traveling salesman theorem for Jordan curves. Advances in Math. 404 (2022), part A, Paper No. 108443, 27 pp.
- [79] C.J. Bishop. Uniformly acute triangulations of PSLGs Discrete & Computational Geometry 70(2023), 1090–1120.
- [80] C.J. Bishop. Uniformly acute triangulations of polygons. to appear *Discrete Comput. Geom.*
- [81] C.J. Bishop, K. Lazebnik and M. Urbanski. Equilateral triangulations and the postcritical dynamics of meromorphic functions. to appear *Math. Annalen*.
- [82] C.J. Bishop. Function theoretic characterizations of Weil-Petersson curves. to appear *Revista Mat. Iberoamericana*, 38 (2022), no. 7, 2355–2384.

- [83] C.J. Bishop and K. Lazebnik. A geometric approach to polynomial and rational approximation. *International Mathematics Research Notices*, Volume 2024, Issue 12, June 2024, Pages 9936–9961.
- [84] C.J. Bishop. Weil-Petersson curves, β -numbers, and minimal surfaces. To appear in Annals of Math..

PREPRINTS

- [85] C.J. Bishop. Non-removable sets for quasiconformal and quasi-isometric mappings in \mathbb{R}^3 .
- [86] C.J. Bishop. Interpolating sequences for the Dirichlet space and its multipliers.
- [87] C.J. Bishop. Distortion of disks by conformal maps.
- [88] C.J. Bishop. A fast quasiconformal mapping theorem for polygons.
- [89] C.J. Bishop. Estimates for harmonic conjugation.
- [90] C.J. Bishop. Another Besicovitch-Kakeya set.
- [91] C.J. Bishop. A curve with no simple crossings by segments.
- [92] C.J. Bishop. Conformal removability is hard.
- [93] C.J. Bishop. BiLipschitz homogeneous hyperbolic nets. Submitted to Annales Fennici Mathematici.
- [94] C.J. Bishop and L. Rempe. Non-compact Riemann surfaces are equilaterally trianguable. Submitted to *Inventiones*.
- [95] C.J. Bishop. Optimal triangulations of polygons. Submitted to Inventiones.
- [96] C.J. Bishop. Wandering domains.
- [97] C.J. Bishop. Equi-triangulation of polygons. Submitted to Amer. Math. Monthly.
- [98] C.J. Bishop and K. Lazebnik. Hilbert's lemniscate theorem for rational functions.
- [99] C.J. Bishop and D.L. Bishop. Approximation by singular polynomial sequences.
- [100] C.J. Bishop, A. Eremenko K. Lazebnik. On the shapes of rational lemniscates. Submitted to GAFA.

BOOKS

- [101] C.J. Bishop and Yuval Peres. Fractals in Analysis and Probability, Cambridge University Press, 2017
- [102] C.J. Bishop and Yuval Peres. Conformal Fractals (in preparation)
- [103] C.J. Bishop. The Riemann Mapping Theorem (in preparation)
- [104] C.J. Bishop. Introduction to Transcendental Dynamics (in preparation)
- [105] C.J. Bishop. Quasiconformal Mappings in the Plane (in preparation)

Copies of my papers and lectures are available at www.math.sunysb.edu/~bishop Email me at bishop@math.stonybrook.edu